

NUMERICAL SIMULATION OF A 3D BILEAFLET MECHANICAL HEART VALVE: FSI COUPLING ALGORITHM

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Abstract. *Bileaflet Mechanical Heart Valves (BMHVs) are preferred for valve replacement. However, current BMHVs induce calcification and thromboembolism which is believed to be related to non-physiological flow. Therefore, numerical flow simulations can provide relevant information for design optimization. Such simulations can be achieved by implementing fluid-structure interaction (FSI).*

In this paper, we present a newly developed FSI coupling algorithm to simulate BMHV dynamics in a partitioned way. The coupling iterations between the flow solver and the leaflet motion solver are accelerated by using the Jacobian with the derivatives of the pressure and viscous moments acting on the leaflets with respect to the leaflet acceleration. This Jacobian is used in the leaflet motion solver when new positions of the leaflets are computed during the coupling iterations. The Jacobian is numerically derived from the flow solver by applying leaflet perturbations. Instead of calculating this Jacobian every time step, the Jacobian is extrapolated from previous time steps and a recalculation of the Jacobian is only done when needed. The convergence process is sped up by the use of extrapolations of angular accelerations and a variable time step size. This time step size depends on the maximum mesh motion, allowing a larger time step when leaflet motion is small and thus reducing the total number of time steps per time cycle. The algorithm is extended to accurately predict correct leaflet movement to and from the closed and opened position.

The algorithm is used to simulate two 3D cases containing a BMHV. One geometry consists of a rigid straight tube. The second geometry is made asymmetrical by adding Valsalva sinuses downstream of the valve. The results show that the leaflets in this second geometry move asynchronously. An algorithm with two degrees of freedom is thus required in an asymmetrical geometry.

1 INTRODUCTION

Bileaflet Mechanical Heart Valves (BMHVs) are widely used and preferred for valve replacement because of their long life span and durability. However, current BMHV designs induce calcification and thromboembolism, which is believed to be due to non-physiological flow and turbulence generated by the valve leaflets [1]. Numerical flow simulations can thus provide relevant information for valve design optimization.

Numerical simulation of such a BMHV is a complex Fluid-Structure Interaction (FSI) problem. The movement of the leaflets strongly interacts with the surrounding fluid motion and therefore it needs to be computed through a coupling scheme. A description of FSI methods for BMHVs can be found in [1]. Unfortunately, when using separate solvers, not every FSI coupling scheme converges efficiently. In literature, the instability of explicit coupling schemes for the case of BMHVs was explained [2,3]. Thus, implicitness is necessary for strong coupling, which implies the introduction of a subiteration loop within each time step. However, for doing so, stable and efficient approximations of the subsequent angular accelerations of the leaflets are needed in each subiteration k .

In this paper, we present a new coupling algorithm, which predicts the moments (and thus the angular accelerations) for the next coupling iteration through a linearization of Newton's Second Law with a numerically computed Jacobian. This method was first introduced in [2,4] for one leaflet, but now extended to two leaflets. The components of the Jacobian are composed of the gradients of the moments (exerted by the flow on the leaflets) with respect to changes in leaflet angular accelerations. Hence, this Jacobian is numerically derived from our flow solver by perturbations of the leaflet positions. Subsequently, the algorithm is extended to perform a correct leaflet movement to and from the closed and the opened position. Finally, the convergence process is accelerated by the use of an adaptive time step size and extrapolation techniques.

The paper is organized as follows. First, we derive the algorithm and analyze its implementation in a commercially available black box flow solver. Subsequently, we test our algorithm on two 3D cases of a BMHV. One geometry consists of a rigid straight tube. The second geometry is made asymmetrical by placing Valsalva sinuses downstream of the valve. Finally, we conclude that our newly developed FSI algorithm for the partitioned simulation of a BMHV is stable and converges efficiently. Also, the results show that the leaflets in the second geometry move asynchronously. An algorithm with two degrees of freedom is thus preferred in an asymmetrical geometry.

2 FSI ALGORITHM

The flow diagram of the algorithm is visualized in figure 1 and will be explained hereafter. The implementation in FLUENT is done by journal files and user-defined functions (UDFs). For each subiteration, the journal file updates the mesh, solves the Navier-Stokes equations and reads the data file of the time step. Thus, this journal file solves the flow problem. The UDFs, on the other hand, simulate the structural part. They perform calculations with the obtained flow solution in order to check for convergence and to set the motion parameters for the next subiteration. They interact with and steer the actions of the journal file. In the following, the steps of the flow diagram are explained and discussed in detail.

2.1 Valve mechanics: leaflet motion solver

A BMHV can be modelled as a rigid casing in which two separate rigid leaflets rotate around their axes. Because the position of each rigid leaflet is solely determined by its opening angle, the valve has two degrees of freedom.

The movement of a rigid leaflet is governed by Newton's Second Law, i.e. the equilibrium between the angular momentum about its hinge and the product of its moment of inertia and its angular acceleration. For two leaflets, this gives the following two equations with M_i , I_i and $\ddot{\theta}_i$ representing, respectively, the angular momentum, the moment of inertia and the angular acceleration of leaflet i about its rotation axis:

$$\begin{cases} M_1 = I_1 \cdot \ddot{\theta}_1 \\ M_2 = I_2 \cdot \ddot{\theta}_2 \end{cases} \quad (1)$$

When the hinges are modelled as frictionless, the angular momentum acting on the leaflet is the pressure (and viscous) momentum exerted by the flow.

As mentioned above, an implicit algorithm is necessary for strong coupling with separate solvers. Within the subiteration process of each time step, implicitness between the subsequent subiterations is needed to obtain fast convergence. Thus, while taking into account the mutual interaction between the leaflets, equation (1) needs to be linearized for each subiteration $k+1$ of time step $n+1$:

$$\begin{cases} M_1^{n+1,k} + \frac{\partial M_1}{\partial \ddot{\theta}_1} (\ddot{\theta}_1^{n+1,k+1} - \ddot{\theta}_1^{n+1,k}) + \frac{\partial M_1}{\partial \ddot{\theta}_2} (\ddot{\theta}_2^{n+1,k+1} - \ddot{\theta}_2^{n+1,k}) = I_1 \cdot \ddot{\theta}_1^{n+1,k+1} \\ M_2^{n+1,k} + \frac{\partial M_2}{\partial \ddot{\theta}_1} (\ddot{\theta}_1^{n+1,k+1} - \ddot{\theta}_1^{n+1,k}) + \frac{\partial M_2}{\partial \ddot{\theta}_2} (\ddot{\theta}_2^{n+1,k+1} - \ddot{\theta}_2^{n+1,k}) = I_2 \cdot \ddot{\theta}_2^{n+1,k+1} \end{cases} \quad (2)$$

These equations can be rearranged as follows:

$$\begin{cases} M_1^{n+1,k} - \frac{\partial M_1}{\partial \ddot{\theta}_1} \ddot{\theta}_1^{n+1,k} - \frac{\partial M_1}{\partial \ddot{\theta}_2} \ddot{\theta}_2^{n+1,k} = I_1 \cdot \ddot{\theta}_1^{n+1,k+1} - \frac{\partial M_1}{\partial \ddot{\theta}_1} \ddot{\theta}_1^{n+1,k+1} - \frac{\partial M_1}{\partial \ddot{\theta}_2} \ddot{\theta}_2^{n+1,k+1} \\ M_2^{n+1,k} - \frac{\partial M_2}{\partial \ddot{\theta}_1} \ddot{\theta}_1^{n+1,k} - \frac{\partial M_2}{\partial \ddot{\theta}_2} \ddot{\theta}_2^{n+1,k} = I_2 \cdot \ddot{\theta}_2^{n+1,k+1} - \frac{\partial M_2}{\partial \ddot{\theta}_1} \ddot{\theta}_1^{n+1,k+1} - \frac{\partial M_2}{\partial \ddot{\theta}_2} \ddot{\theta}_2^{n+1,k+1} \end{cases} \quad (3)$$

This can be written in matrix notation:

$$\begin{bmatrix} M_1^{n+1,k} - \frac{\partial M_1}{\partial \ddot{\theta}_1} \ddot{\theta}_1^{n+1,k} - \frac{\partial M_1}{\partial \ddot{\theta}_2} \ddot{\theta}_2^{n+1,k} \\ M_2^{n+1,k} - \frac{\partial M_2}{\partial \ddot{\theta}_1} \ddot{\theta}_1^{n+1,k} - \frac{\partial M_2}{\partial \ddot{\theta}_2} \ddot{\theta}_2^{n+1,k} \end{bmatrix} = \begin{bmatrix} I_1 - \frac{\partial M_1}{\partial \ddot{\theta}_1} & -\frac{\partial M_1}{\partial \ddot{\theta}_2} \\ -\frac{\partial M_2}{\partial \ddot{\theta}_1} & I_2 - \frac{\partial M_2}{\partial \ddot{\theta}_2} \end{bmatrix} \cdot \begin{bmatrix} \ddot{\theta}_1^{n+1,k+1} \\ \ddot{\theta}_2^{n+1,k+1} \end{bmatrix} \quad (4)$$

or

$$[M]^{n+1,k} = [A] \cdot [\ddot{\theta}]^{n+1,k+1} \quad (5)$$

Thus, the matrix $[\ddot{\theta}]^{n+1,k+1}$ contains the angular accelerations on time step $n+1$ and subiteration $k+1$. The matrix $[A]$ is composed of the moments of inertia and the derivatives of the moments with respect to angular acceleration (i.e. the Jacobian). Finally, the matrix $[M]^{n+1,k}$ consists of all the remaining factors (in time step $n+1$ and subiteration k).

For a well-posed problem, the matrix $[A]$ is nonsingular. So the previous equation can be rewritten as:

$$[\ddot{\theta}]^{n+1,k+1} = [A]^{-1} \cdot [M]^{n+1,k} \quad (6)$$

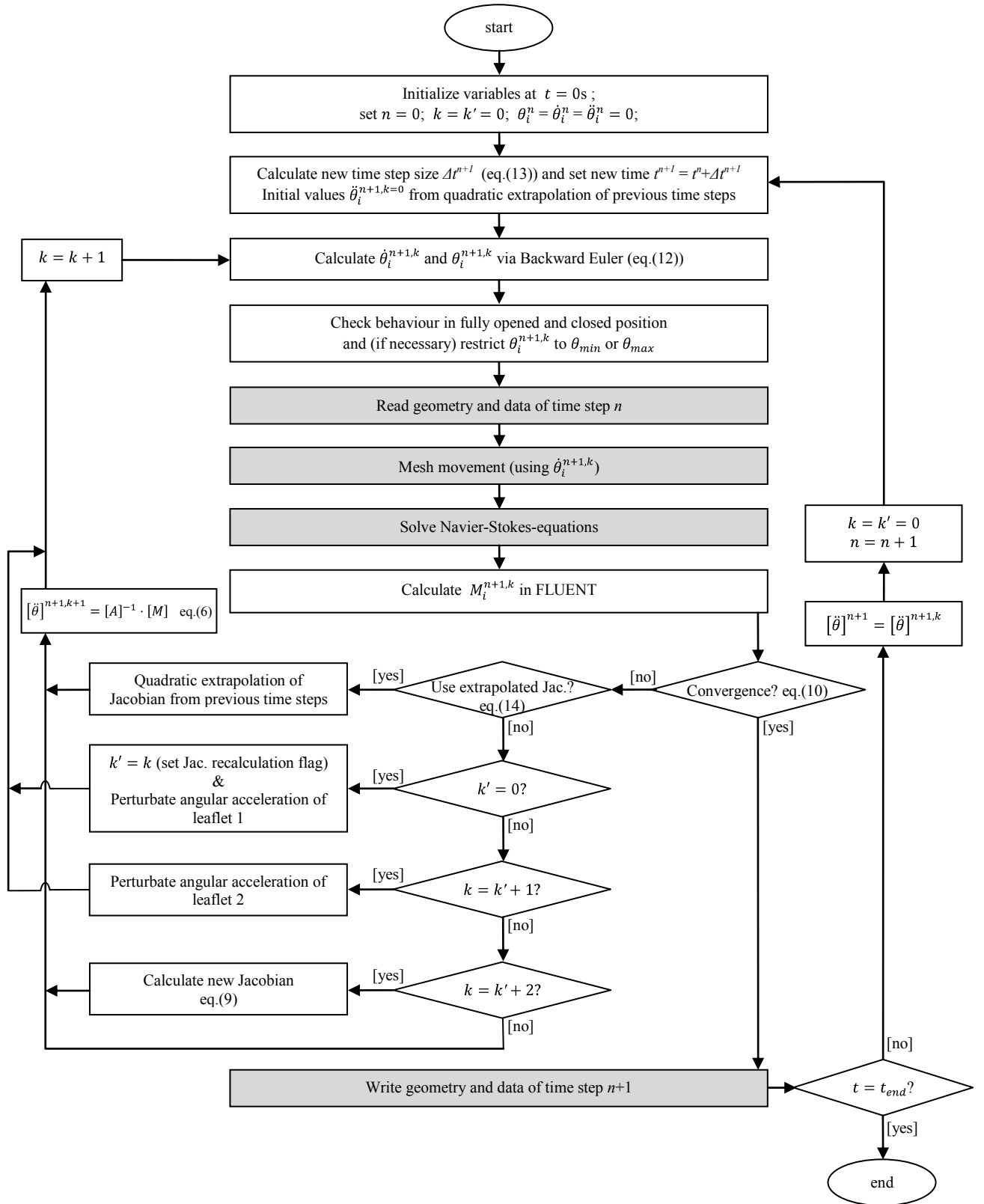


Figure 1: Flow diagram of implicit FSI coupling algorithm with two degrees of freedom.
 n = time step, k = subiteration step, k' = Jacobian recalculation flag, i = leaflet number.
 Shaded: executed using generated journal file. Unshaded: executed using compiled UDFs.

2.2 Estimating the Jacobian and calculating the leaflet motions

In order to solve equation (6) and to calculate the angular accelerations of the new subiteration, the Jacobian has to be known. However, when a black box flow solver is used, these derivatives are unknown, but can be approximated by finite differences. Therefore, three subiterations are needed within each time step. The first recalculation subiteration is the reference. We denote this subiteration by setting $k' = k$, i.e. setting the ‘‘Jacobian recalculation flag’’. In the second and third recalculation subiteration ($k = k'+1$ and $k = k'+2$), a small perturbation δ is subsequently induced to the angular acceleration of each of the leaflets, while keeping the other one fixed. The value of this perturbation parameter δ ranges between a minimal value (in order to obtain a significant difference between the ‘‘reference moment’’ and the ‘‘perturbation moment’’) and a maximal value (above which the mesh motion could fail). In [2], it was shown that the exact choice of this parameter is not very sensitive.

For each Jacobian recalculation subiteration, the moments acting on the leaflets are calculated and stored. This can be summarized as follows:

$$\begin{aligned}
 k = k' &\Rightarrow \begin{cases} \ddot{\theta}_1^{n+1,k=k'} \\ \ddot{\theta}_2^{n+1,k=k'} \end{cases} \Rightarrow \begin{cases} M_1^{n+1,k=k'} \\ M_2^{n+1,k=k'} \end{cases} \\
 k = k'+1 &\Rightarrow \begin{cases} \ddot{\theta}_1^{n+1,k=k'+1} = \ddot{\theta}_1^{n+1,k=k'} + \delta \\ \ddot{\theta}_2^{n+1,k=k'+1} = \ddot{\theta}_2^{n+1,k=k'} \end{cases} \Rightarrow \begin{cases} M_1^{n+1,k=k'+1} \\ M_2^{n+1,k=k'+1} \end{cases} \\
 k = k'+2 &\Rightarrow \begin{cases} \ddot{\theta}_1^{n+1,k=k'+2} = \ddot{\theta}_1^{n+1,k=k'} \\ \ddot{\theta}_2^{n+1,k=k'+2} = \ddot{\theta}_2^{n+1,k=k'} + \delta \end{cases} \Rightarrow \begin{cases} M_1^{n+1,k=k'+2} \\ M_2^{n+1,k=k'+2} \end{cases} \quad (7)
 \end{aligned}$$

The derivatives are estimated using finite differences ($i, j = 1, 2$):

$$\frac{\partial M_i}{\partial \ddot{\theta}_j} \approx \frac{\Delta M_i}{\Delta \ddot{\theta}_j} \quad (8)$$

This gives for each component of the Jacobian:

$$\begin{aligned}
 \frac{\partial M_1}{\partial \ddot{\theta}_1} &\approx \frac{\Delta M_1}{\Delta \ddot{\theta}_1} = \frac{M_1^{n+1,k=k'+1} - M_1^{n+1,k=k'}}{\ddot{\theta}_1^{n+1,k=k'+1} - \ddot{\theta}_1^{n+1,k=k'}} = \frac{M_1^{n+1,k=k'+1} - M_1^{n+1,k=k'}}{\delta} \\
 \frac{\partial M_1}{\partial \ddot{\theta}_2} &\approx \frac{\Delta M_1}{\Delta \ddot{\theta}_2} = \frac{M_1^{n+1,k=k'+2} - M_1^{n+1,k=k'}}{\ddot{\theta}_2^{n+1,k=k'+2} - \ddot{\theta}_2^{n+1,k=k'}} = \frac{M_1^{n+1,k=k'+2} - M_1^{n+1,k=k'}}{\delta} \\
 \frac{\partial M_2}{\partial \ddot{\theta}_1} &\approx \frac{\Delta M_2}{\Delta \ddot{\theta}_1} = \frac{M_2^{n+1,k=k'+1} - M_2^{n+1,k=k'}}{\ddot{\theta}_1^{n+1,k=k'+1} - \ddot{\theta}_1^{n+1,k=k'}} = \frac{M_2^{n+1,k=k'+1} - M_2^{n+1,k=k'}}{\delta} \\
 \frac{\partial M_2}{\partial \ddot{\theta}_2} &\approx \frac{\Delta M_2}{\Delta \ddot{\theta}_2} = \frac{M_2^{n+1,k=k'+2} - M_2^{n+1,k=k'}}{\ddot{\theta}_2^{n+1,k=k'+2} - \ddot{\theta}_2^{n+1,k=k'}} = \frac{M_2^{n+1,k=k'+2} - M_2^{n+1,k=k'}}{\delta} \quad (9)
 \end{aligned}$$

For the following subiterations ($k \geq k'+3$), the angular accelerations can now be calculated by equation (6) until the FSI convergence criterion is satisfied. For each leaflet i , this FSI convergence criterion is given by:

$$\left| M_i^{n+1,k} - I_i \cdot \ddot{\theta}_i^{n+1,k} \right| < \varepsilon \quad (10)$$

The convergence threshold ε is set at one percent of $M_i^{n+1,k}$:

$$\varepsilon = \frac{M_i^{n+1,k}}{100} \quad (11)$$

When the FSI convergence criterion is satisfied, the geometry and data of the time step are stored and the next time step is initiated.

From the angular acceleration obtained from equation (6), the angular velocity and position of each leaflet on the time level $t + \Delta t$ is calculated using a time-integration scheme. Because the flow solver uses a backward Euler scheme, this scheme is also preferred for the structural solver, as shown in [2],

$$\begin{cases} \ddot{\theta}_i^{n+1,k+1} = \frac{\dot{\theta}_i^{n+1,k+1} - \dot{\theta}_i^n}{\Delta t} \\ \dot{\theta}_i^{n+1,k+1} = \frac{\theta_i^{n+1,k+1} - \theta_i^n}{\Delta t} \end{cases} \Rightarrow \begin{cases} \dot{\theta}_i^{n+1,k+1} = \dot{\theta}_i^n + \Delta t \cdot \ddot{\theta}_i^{n+1,k+1} \\ \theta_i^{n+1,k+1} = \theta_i^n + \Delta t \cdot \dot{\theta}_i^n + \Delta t^2 \cdot \ddot{\theta}_i^{n+1,k+1} \end{cases} \quad (12)$$

2.3 Adaptive time step size

The maximum allowable time step size is restricted by the maximum allowable mesh motion, and thus by grid characteristics. A criterion based on the maximum leaflet movement can be posted:

$$\dot{\theta}_i^n \cdot \Delta t^{n+1} \leq \Delta \theta_{\max} \quad \Rightarrow \quad \Delta t^{n+1} \leq \frac{\Delta \theta_{\max}}{\dot{\theta}_i^n} \quad (13)$$

2.4 Quadratic extrapolations from previous time steps

When advancing to a new time step, the angular accelerations for the first subiteration ($k = 0$) are estimated based on a quadratic extrapolation from previous time steps. This prediction of the initial values results in faster convergence.

Also, instead of calculating the Jacobian every time step, the Jacobian is quadratically extrapolated from previous time steps and used in the subiterations $k \geq 1$. Thus, the recalculation of the Jacobian is only done when needed. This recalculation is triggered when the residual drop of our FSI convergence criterion becomes too small. In our case, an arbitrary criterion of one order of magnitude in residual drop between two subsequent subiterations is set.

This can be summarized as follows:

- $k = 0$: extrapolation of angular accelerations and check FSI convergence criterion (equation (10));
- $k \geq 1$: angular accelerations from equation (6) with extrapolated Jacobian and check FSI convergence criterion (equation (10)), until

$$\left| M_i^{n+1,k} - I_i \cdot \ddot{\theta}_i^{n+1,k} \right| > \frac{\left| M_i^{n+1,k-1} - I_i \cdot \ddot{\theta}_i^{n+1,k-1} \right|}{10} \quad (14)$$

from then on, we set $k' = k$ and perform two subiterations to recalculate the Jacobian:

- $k = k'+1$: perturbate angular acceleration of leaflet 1 with δ ;
- $k = k'+2$: perturbate angular acceleration of leaflet 2 with δ ;
- $k \geq k'+3$: angular accelerations from equation (6) with the newly calculated Jacobian and check FSI convergence criterion (equation (10)).

2.5 Behavior in fully opened and fully closed position

The angular position of a leaflet is restricted by a minimum and a maximum angle, respectively the fully closed and fully opened position. In reality, this is usually done by a physical blocking mechanism incorporated in the design of the hinges.

Numerically, these limitations can be modelled by setting the position equal to the restriction and recalculating the angular velocity and acceleration. This is implemented

as follows. When the calculated position of a leaflet exceeds its limitations (i.e. $\theta_i^{n+1,k+1} < \theta_{\min}$ or $\theta_i^{n+1,k+1} > \theta_{\max}$), then the position is set equal to this limit (i.e. $\theta_i^{n+1,k+1} = \theta_{\min}$ or $\theta_i^{n+1,k+1} = \theta_{\max}$). In order to move exactly to the limited position in the time step, the angular velocity $\dot{\theta}_i^{n+1,k+1}$ and acceleration $\ddot{\theta}_i^{n+1,k+1}$ are subsequently recalculated (using the backward Euler scheme):

$$\begin{aligned}\theta_i^{n+1,k+1} &= \theta_{\min} \text{ or } \theta_{\max} \\ \dot{\theta}_i^{n+1,k+1} &= \frac{\theta_i^{n+1,k+1} - \theta_i^n}{\Delta t} \\ \ddot{\theta}_i^{n+1,k+1} &= \frac{\dot{\theta}_i^{n+1,k+1} - \dot{\theta}_i^n}{\Delta t}\end{aligned}\quad (15)$$

However, the previously described FSI convergence criterion must be changed when the position is limited. The FSI convergence criterion should no longer depend on the absolute value of $M_i^{n+1,k} - I_i \cdot \ddot{\theta}_i^{n+1,k}$, but merely on its sign. This can be understood by adding M_i^r to the angular momentum equation, with M_i^r being the reaction moment of the blocking mechanism exerted on the leaflets:

$$M_i^r + M_i^{n+1,k} = I_i \cdot \ddot{\theta}_i^{n+1,k} \quad (16)$$

or

$$M_i^r = -(M_i^{n+1,k} - I_i \cdot \ddot{\theta}_i^{n+1,k}) \quad (17)$$

In order to maintain contact between the leaflet and the blocking mechanism, this reaction moment will be either negative or positive (depending on the case: θ_{\min} or θ_{\max}). As FSI convergence criterion, it is checked whether or not the reaction moment has this appropriate sign. So when the motion of leaflet i is limited, the FSI convergence criterion (equation (10)) of this leaflet i is replaced by

$$M_i^r < 0 \quad (18)$$

or

$$M_i^r > 0 \quad (19)$$

depending on the orientation of the leaflet and on whether the leaflet is fully opened or fully closed.

3 NUMERICAL SIMULATION OF A 3D BMHV

The described algorithm is implemented in FLUENT to simulate two 3D cases. The used BMHV is a model of the 25mm ATS Open Pivot Standard Heart Valve in aortic position. The orifice inner diameter measures 20.8mm. The valve is simplified at the hinge regions. In several studies [4,5], the leaflets are scaled to 98% of their original size. In this paper, no such downscaling is applied to the leaflets. Thus, a realistic gap size between leaflet and casing is maintained.

Furthermore, the first geometry consists of a rigid straight tube and is visualized in figure 2. The second geometry consists also of a rigid straight tube upstream of the valve, but rigid Valsalva sinuses are added downstream of the valve (figure 3). The Valsalva sinuses are based on the geometry described in [6] and positioned asymmetrically with respect to the leaflets. It is expected that this asymmetrical geometry induces an asymmetric flow field downstream of the valve, resulting in an asynchronous motion of the valve leaflets. Therefore, it is an effective test for our algorithm with two degrees of freedom.

An unstructured grid is generated in the geometry and the arbitrary Lagrangian-Eulerian (ALE) approach is followed, which implies that the grid follows the motion of the structure and therefore needs an update. If applicable, this update is done using dynamic remeshing and spring smoothing.

An inlet aortic flow pulse with a time cycle of 1s (displayed in figure 5) is imposed upstream. Since in a rigid tube geometry the pressure level does not affect the flow field (only the pressure gradient appears in the equation), a constant pressure is imposed at the downstream outlet boundary. Blood is modelled as a laminar incompressible fluid and a no-slip condition is applied at the walls. The valve is initially set in the closed position.

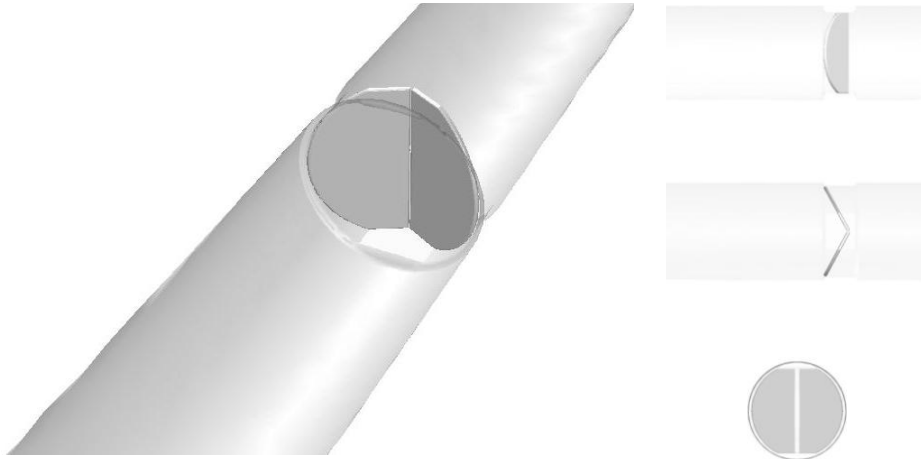


Figure 2: View on the first geometry, with straight tube downstream of the valve: seen isometric (*left*), from front (*up*), from top (*middle*) and from inlet (*down*).

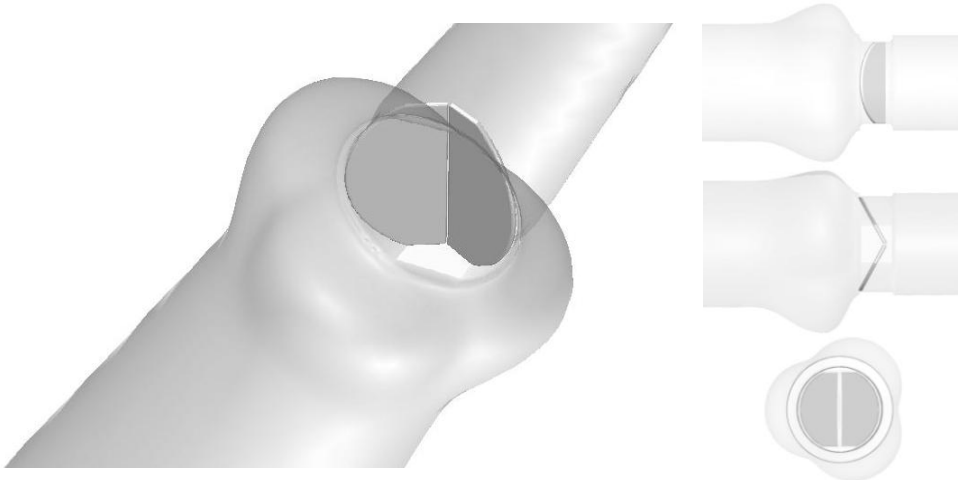


Figure 3: View on the second geometry, with Valsalva sinuses downstream of the valve: seen isometric (*left*), from front (*up*), from top (*middle*) and from inlet (*down*).

The solution process shows that the algorithm is stable and efficient. For each time step, it reaches convergence within a few subiterations. The results of the simulations are depicted in figure 4 and figure 6, which show the velocity magnitudes and static pressure contours for the two geometries. The flow pattern consists of three jets, which is typical for a BMHV.

Figure 5 presents the angular positions of the leaflets, in which 0 rad and 0.988 rad respectively refers to the fully closed and fully opened position. However, the results show that this maximum opening angle is not reached in the second geometry (with Valsalva sinuses). Such incomplete opening is typical for the ATS Open Pivot valve in a divergent geometry and is described in literature. In [7], this phenomenon was

explained due to the greater sensitivity of the leaflet movement to the flow field compared to other BMHV designs, since the leaflets extend farther in the flow downstream of the orifice than is the case in other designs. Therefore, the valve did not open completely in the divergent transvalvular flow (caused by the Valsalva sinuses enlargement). In the straight tube, however, a full opening of the valve leaflets is observed.

Also, it is found that the two leaflets show differences in movement for the Valsalva sinuses geometry. As mentioned above, it can be understood that this asynchrony is triggered by the presence of the asymmetric geometry downstream of the valve. In the straight tube geometry, no differences in movement are found.

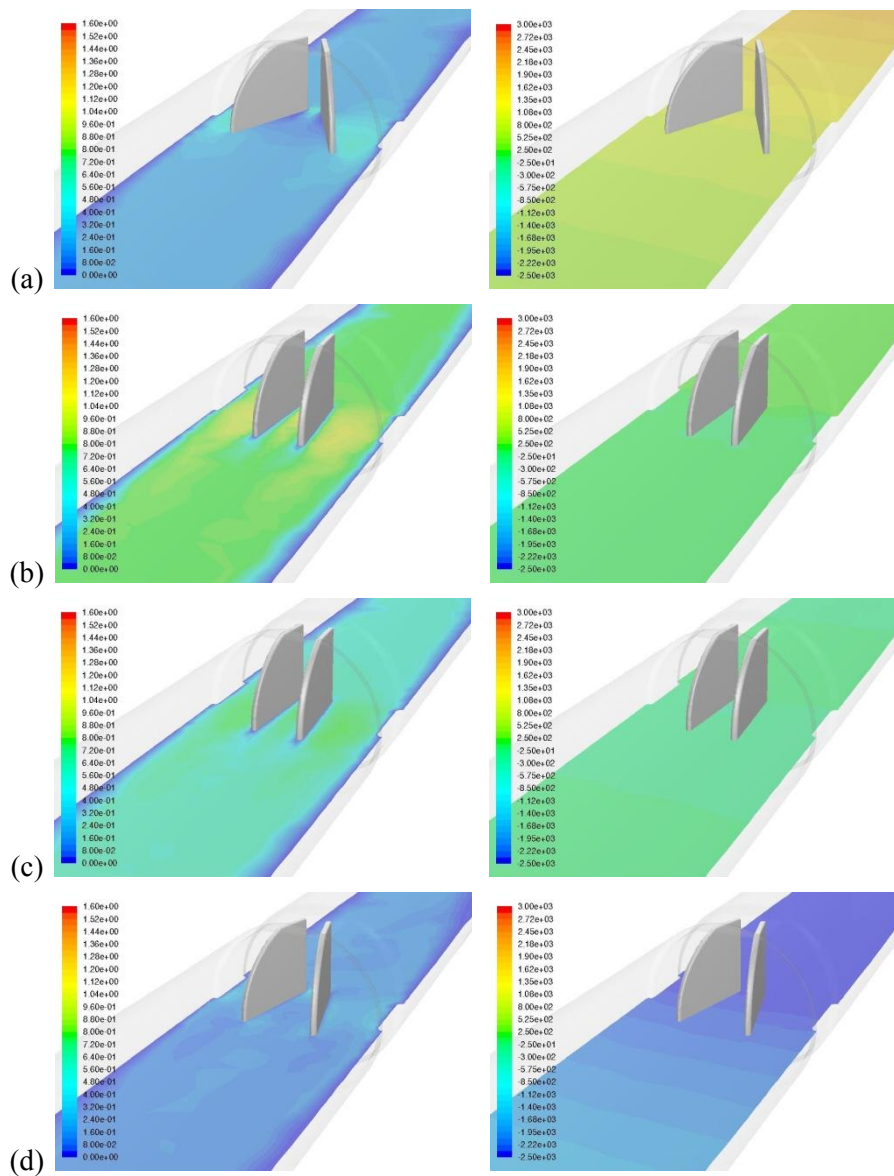


Figure 4: Velocity Magnitude Contours in m/s (*left*) and Static Pressure Contours in Pa (*right*) for the first geometry (straight tube), visualized on a longitudinal section perpendicular to the leaflet rotation axes, at $t = 0.025s$ (*a*), $t = 0.125s$ (*b*), $t = 0.250s$ (*c*) and $t = 0.375s$ (*d*), represented by respectively the purple, red, green and blue dot in figure 5.

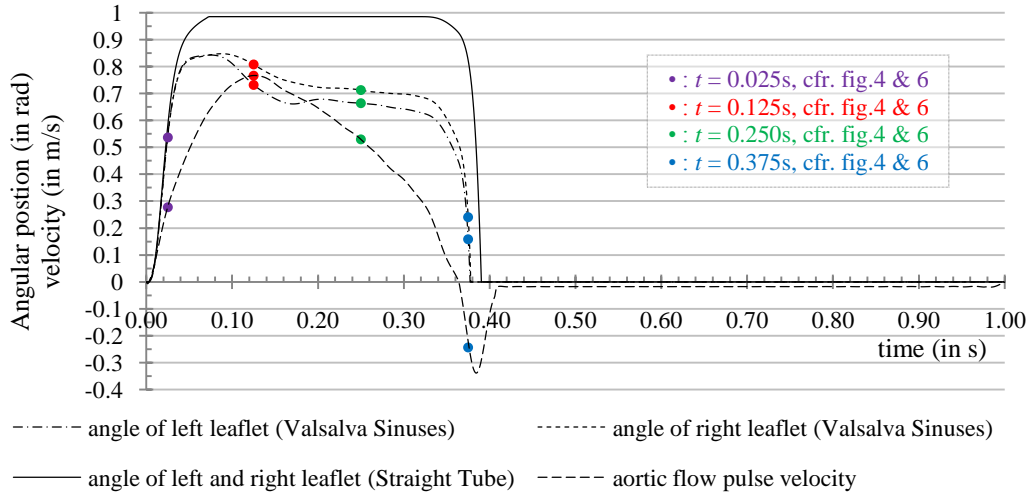


Figure 5: Angular position of leaflets and aortic flow pulse velocity.

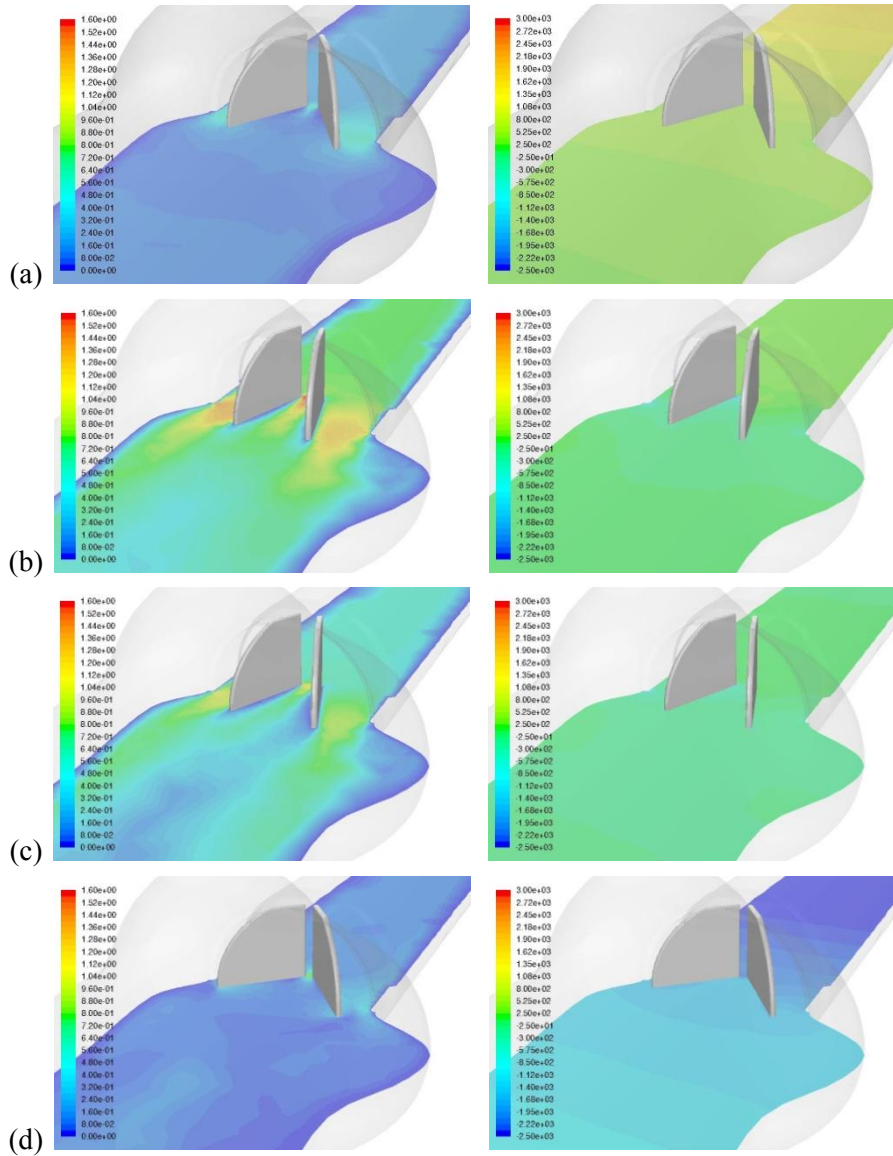


Figure 6: Velocity Magnitude Contours in m/s (*left*) and Static Pressure Contours in Pa (*right*) for the second geometry (Valsalva sinuses), visualized on a longitudinal section perpendicular to the leaflet rotation axes, at $t = 0.025s$ (a), $t = 0.125s$ (b), $t = 0.250s$ (c) and $t = 0.375s$ (d), represented by respectively the purple, red, green and blue dot in figure 5.

4 CONCLUSIONS

A new implicit FSI coupling algorithm for the partitioned simulation of a BMHV was presented. The coupling iterations between the flow solver and the leaflet motion solver are accelerated by using the (numerically derived) Jacobian with the derivatives of the pressure and viscous moments acting on the leaflets with respect to the leaflet acceleration. The algorithm was stable and converged efficiently.

Furthermore, it was successfully tested and implemented for two 3D cases of a BMHV. The results showed that the leaflets in an asymmetric geometry move asynchronously. In such cases, an algorithm with two degrees of freedom is thus required.

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