

# STRESS-STRAIN MODELLING OF HEATED CONCRETE

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## ABSTRACT

This paper presents a stress-strain model of heated concrete [1,2] based on extensive testing carried out by the third author on the strain behaviour of concrete during two heat cycles to temperatures up to 600°C [3-7]. Strain measurements of three concretes during two cycles of heating with and without compressive load over a period of 14 days allow the identification, and separation, of strain components for the transient and steady state temperature conditions as functions of temperature. Contractive strain components during first heating are dominated by the Load Induced Thermal Strain (LITS) with shrinkage being the second strain component. The contractive strains during the subsequent period at constant temperature comprises both creep and shrinkage. The former would contain delayed Transient creep (relevant to the temperature in question) as well as constant temperature creep. While LITS is absent during cooling and subsequent thermal cycle, another important strain component appears which is expansive and which is related to the cracks that develop during cooling and subsequent thermal cycle. These crack strains depend on the type of concrete, the temperature level and the load level. The residual strain is measured directly and modelled indirectly as the sum of the irrecoverable contractive and expansive components. The comprehensive strain model obtained from the tests is then directly integrated in the mechanical part of a 3D fully coupled thermo-hydro-mechanical numerical model of heated concrete, developed by the first two authors, described in this paper along with the test results [8-14]. The generated F.E. code is called NEWCON. Concrete is treated as a multiphase system where the voids of the skeleton are partly filled with liquid and partly with a gas phase [15-17]. As regards the mechanical field, NEWCON couples creep and shrinkage [18-25], chemo-thermo-mechanical damage [26-30] and plasticity effects under medium and high temperature levels.

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