

GENERALIZED ROTATION PARAMETERS FOR THE NONLINEAR ANALYSIS OF ROD AND SHELLS

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ABSTRACT

This work presents a generic formulation of vector-type for the parameterization of large rotations in three-dimensional space. Special distinction is made to the here named “generalized Rodrigues parameters”, which result in simple and computationally efficient expressions.

The parameterization is introduced into the rod and shell models of [1,2,3,4,5]. However, in contrast to these works, the weak forms are constructed here with both orthogonal and non-orthogonal projections, corresponding to the application of the virtual work theorem or virtual power theorem respectively (see [6]). We show the pros and cons of each of these projections in connection with the adopted rotation parameterization. Issues as the objectivity of the finite element model, formulas for the rotation composition and the size of the rotation increments are thereby discussed.

The formulation is implemented within a finite element code and assessment of the scheme is made by means of several numerical simulations.

REFERENCES

- [1] Pimenta PM, Yoho T, “Geometrically-exact analysis of spatial frames”, Applied Mechanics Reviews, ASME, New York, v.46, 11, 118-128, 1993.
- [2] Pimenta PM, “Geometrically-Exact Analysis of Initially Curved Rods”, in: Advances in Computational Techniques for Structural Engineering, Edinburgh, U.K., v.1, 99-108, Civil-Comp Press, Edinburgh, 1996.
- [3] Campello EMB, Pimenta PM and Wriggers P, “A triangular finite shell element based on a fully nonlinear shell formulation”, Comput. Mech., 31 (6), 505-518, 2003.

- [4] Pimenta PM, Campello EMB and Wriggers P, “A fully nonlinear multi-parameter shell model with thickness variation and a triangular shell finite element”, *Comput. Mech.*, 34 (3), 181-193, 2004.
- [5] Pimenta PM, Campello EMB, Wriggers P, “Shell curvature as an initial deformation: geometrically exact finite element approach”, submitted to *Int. J. Num. Meth. Engng.* 2007.
- [6] Pimenta PM, Campello EMB, Wriggers P, “An exact conserving algorithm for nonlinear dynamics with rotational DOFs and general hyperelasticity. Part 1: Rods”. Submitted to *Computational Mechanics*.