

SOLUTION OF MELTING PROBLEMS BY A MESHLESS TECHNIQUE

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Key Words: *Melting, Local Radial Basis Function Collocation, Multiquadrics, Gobin - Le Quéré Test Case.*

ABSTRACT

This paper explores the application of the mesh-free Local Radial Basis Function Collocation Method (LRBFCM) [1] in solution of coupled heat transfer and fluid flow problems [2,3] associated with meeting of a pure substance [4]. The problem is formulated within the one-domain mixture-enthalpy framework and the phase-change of a pure substance is modelled through a narrow temperature interval. The involved temperature, velocity and pressure fields are represented on overlapping sub-domains through collocation by using multiquadrics Radial Basis Functions (RBF). The involved first and second derivatives of the fields are calculated from the respective derivatives of the RBF's. The energy and momentum equations are solved through explicit time stepping. The pressure-velocity coupling is calculated iteratively, with pressure correction, predicted from the local continuity equation violation. The pressure correction is entirely local and does not require solution of pressure Poisson or pressure correction Poisson equations. The solution procedure is represented for Gobin Le Quéré melting benchmark spectra for tin at Stefan number (Ste) 0.01, Prandtl number (Pr) 0.02, and Rayleigh numbers (Ra) 2.5e4, 2.5e4 and paraffin with Ste = 0.1, Pr = 50, and Ra = 10e7, 10e8. The results of the present method are compared with the results of other combinations of different numerical methods and formulations which attempted this benchmark in the past. The results of the novel method compare well with other contributions. The advantages of the new method are its simplicity, accuracy and straightforward applicability in non-uniform node arrangements.

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