

FreeFem++: a versatile tool to solve optimization problem in finite element methods

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ABSTRACT

I will present FreeFem++ and how to use to build a optimization process in CFD. This optimization example is the classic reduction drag problem around a multi-corp wing. We will all show how to add novel technics as mesh adaptation with anisotropy , fast sparse linear solver.

FreeFem++ is a free software to solve bidimensional and tridimensional PDE's and the characteristics of FreeFem++ are:

- Problem description (real or complex valued) by their variational formulations, with access to the internal vectors and matrices if needed.
- Multi-variables, multi-equations, static or time dependent, linear or nonlinear coupled systems; however the user is required to describe the iterative procedures which reduce the problem to a set of linear problems.
- Easy geometric input by analytic description of boundaries by pieces in 2d; however this software is not a CAD system; for instance when two boundaries intersect, the user must specify the intersection points.
- Automatic mesh generator, based on the Delaunay-Voronoi algorithm in 2d. Inner point density is proportional to the density of points on the boundary [1].
- Metric-based anisotropic mesh adaptation in 2d. The metric can be computed automatically from the Hessian of any FreeFem++ function [2].
- High level user friendly typed input language with an algebra of analytic and finite element functions.
- Multiple finite element meshes within one application with automatic interpolation of data on different meshes and possible storage of the interpolation matrices.
- A large variety of triangular finite elements : linear and quadratic Lagrangian elements, discontinuous P1 and Raviart-Thomas elements, elements of a non-scalar type, mini-element, . . . (but no quadrangles).
- Tools to define discontinuous Galerkin formulations via finite elements P0, P1dc, P2dc and keywords: jump, mean, intalldges.

- A large variety of linear direct and iterative solvers (LU, Cholesky, Crout, CG, GMRES, UMFPACK) and eigenvalue and eigenvector solvers.
- Near optimal execution speed (compared with compiled C++ implementations programmed directly).
- Online graphics, generation of .txt,.eps,.gnu, mesh files for further manipulations of input and output data.
- Many examples and tutorials: elliptic, parabolic and hyperbolic problems, Navier-Stokes flows, elasticity, Fluid structure interactions, Schwarz's domain decomposition method, eigenvalue problem, residual error indicator, ...
- An parallel version using mpi

REFERENCES

- [1] F. Hecht, *The mesh adapting software: bamg*, INRIA report, on the web at <http://www-rocq.inria.fr/gamma/cdrom/www/bamg/eng.htm>, (1998).
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