



and fast boundary element computation. The proposed solution exploits the surface discretization nature of BEM, and eliminates time-consuming NURBS surface/solid reconstruction needed in a domain approach. In the developed BEM, unstructured as-scanned data can be directly imported and regularized into a BEM mesh. A simple mesh regularization procedure is implemented to ensure quality of the translated BEM mesh. The developed BEM achieves a near order  $N$  computational complexity, by coupling the conventional BEM (of order  $N^3$ ) with the fast multipole acceleration [4, 5].

Numerical examples are presented to demonstrate the effectiveness and efficiency of the developed BEM. Preliminary results show that the developed BEM can be a promising tool for reverse engineering simulation applications involving highly complex organic shapes and large-scale models (Figure 1), e.g., the ones acquired from medical images.

The image-based BEM with FMM acceleration, though only developed for steady-state thermal analysis in this study, can be readily extended for elasticity. Multiple material domains with interface effects can also be considered. With further development, more interesting numerical experiments can be conducted, e.g. virtual tensile, compressive or bending testing of realistic high-resolution digital objects. Modeling results of these studies can then be used for prediction and characterization, e.g., biomechanical behaviors from patient-specific scan images. The image-based BEM, once fully-developed, will have many promising applications in areas including material science, biomedical engineering, and traditional design.

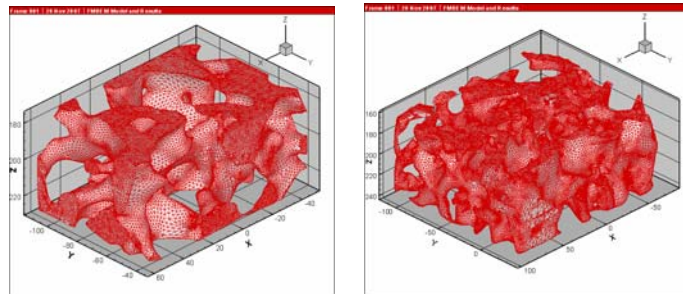


Figure 1. BEM models for healthy and weak trabecular bone microstructures

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