

# POPULATION TRANSFER PROCESSES: FROM ATOMS TO CLUSTERS AND BOSE-EINSTEIN CONDENSATE

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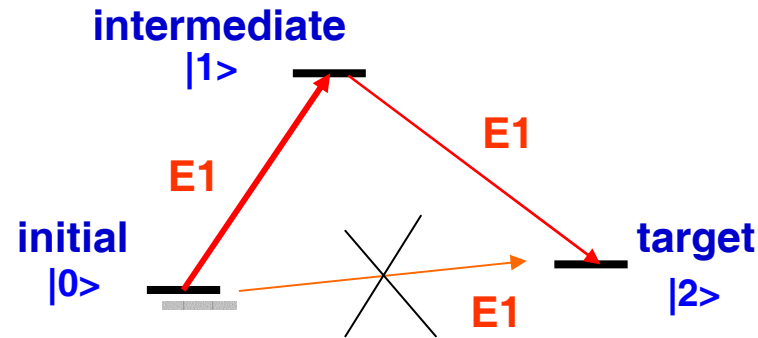
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**Typical problem of atomic/molecular spectroscopy:**  
how to provide the population transfer between the levels which **cannot** be directly related by **dipole** transition?



**Modern quantum optics:** various methods for **two-photon population transfer** in atoms and simple molecules:

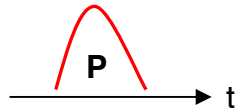
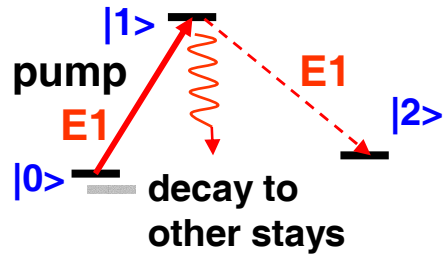
- Raman scattering,
- stimulated Raman,
- Rapid Adiabatic Passage (RAP)
- STimulated Raman Adiabatic Passage (STIRAP),
- Stark-shift-Chirped Rapid Adiabatic Passage (SCRAP),
- ....

**Is it possible to use these methods for other systems:**

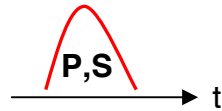
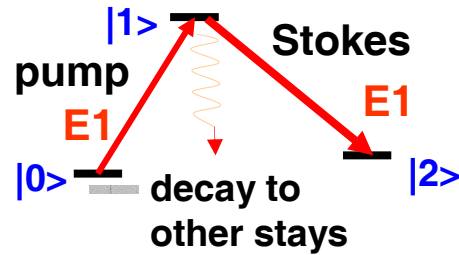
- exploration of electronic of metal clusters
- transport of BEC



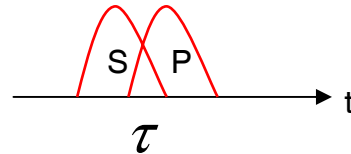
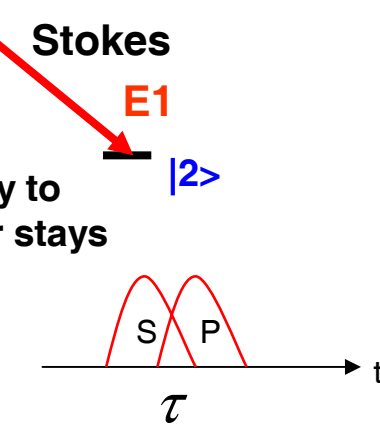
# Two-photon population transfer methods:



**Simple Raman scattering:**  
 - only pump  
 - low transfer



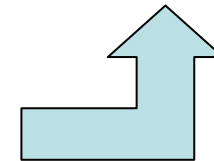
**Stimulated Raman scattering:**  
 - pump + Stokes  
 - transfer up to 30%



**STimulated Raman Adiabatic Passage (STIRAP):**  
 - Stokes + pulse  
 - transfer up to **100% !!!**

K. Bergman, et al,  
 Rev. Mod. Phys., 70, 1003 (1998)

- adiabatic process
- counterintuitive pulse order
- partial overlap
- dark state



## Dressed states in STIRAP:

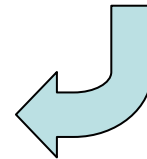
$$|a^+\rangle = \sin\theta \sin\phi |0\rangle + \cos\phi |1\rangle + \cos\theta \sin\phi |2\rangle$$

$$|a^0\rangle = \cos\theta |0\rangle + \sin\theta |2\rangle \quad \leftarrow \text{dark state}$$

$$|a^-\rangle = \sin\theta \cos\phi |0\rangle + \sin\phi |1\rangle + \cos\theta \cos\phi |2\rangle$$

$\left\{ \begin{array}{l} = |0\rangle \text{ at } t=0 \\ = |2\rangle \text{ at } t=\infty \end{array} \right.$

$$\sin\theta = \frac{\Omega_P}{\sqrt{\Omega_P^2(t) + \Omega_S^2(t)}}, \quad \cos\theta = \frac{\Omega_S}{\sqrt{\Omega_P^2(t) + \Omega_S^2(t)}}$$



Is it possible to apply the fascinating methods  
of modern quantum optics to:

- exploration of electronic spectra in metal clusters,
- transport of BEC in multi-well traps or  
between BEC components



Atomic clusters: why not?

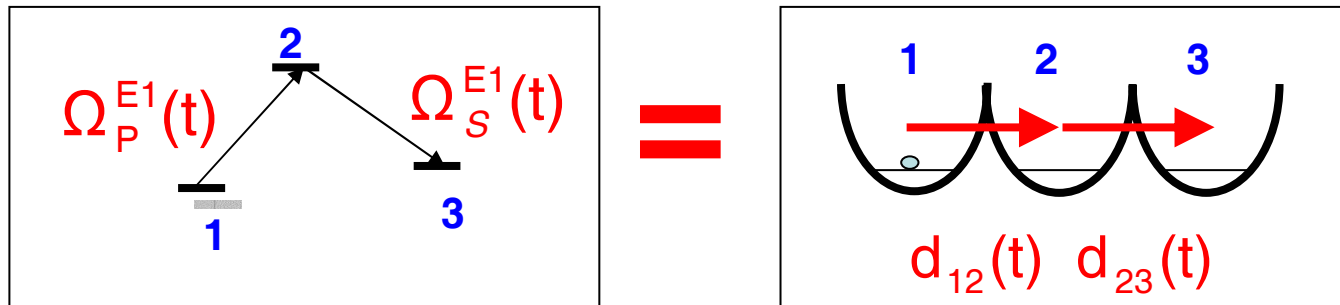
But the problems of:

- extremely short lifetimes (10-1000 fs),
- competition with plasmon mode,
- strong dynamical stark shifts from  
intense pulses

Transport of

Bose-Einstein condensate: why yes?

Because TPP and BEC tunneling  
are similar physically and mathematically!

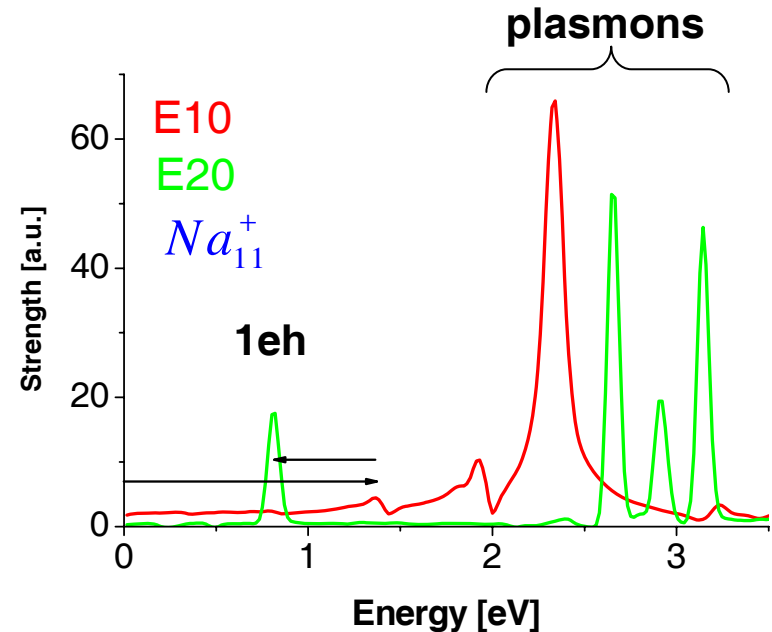
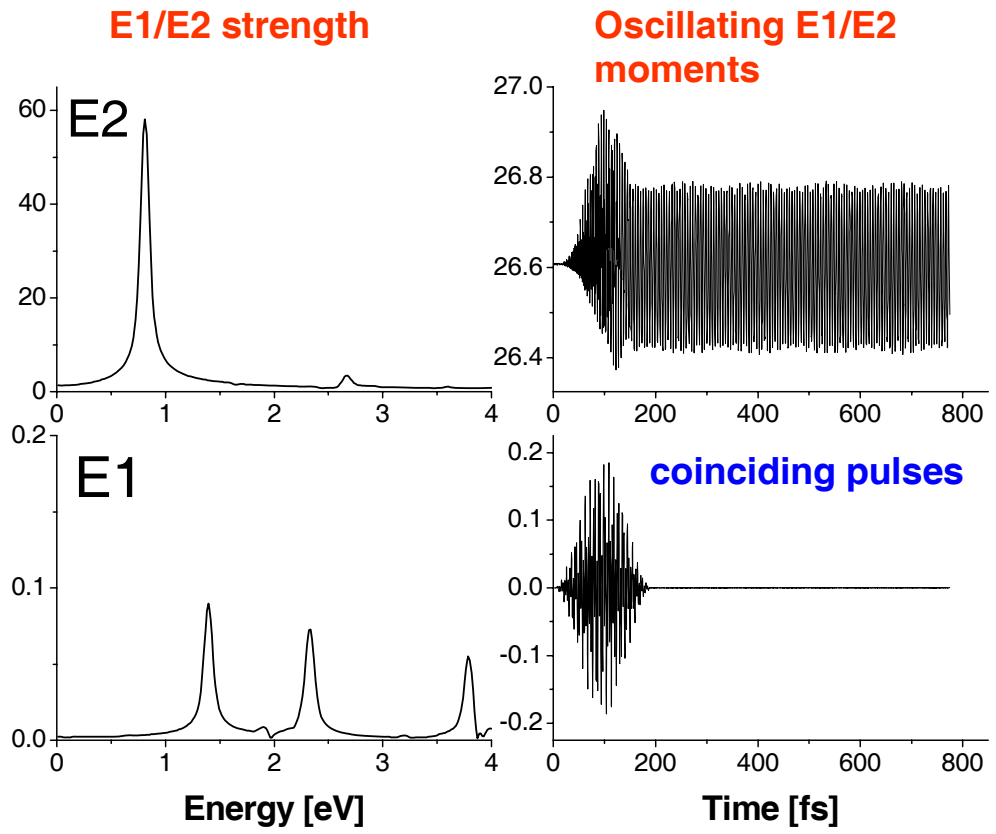
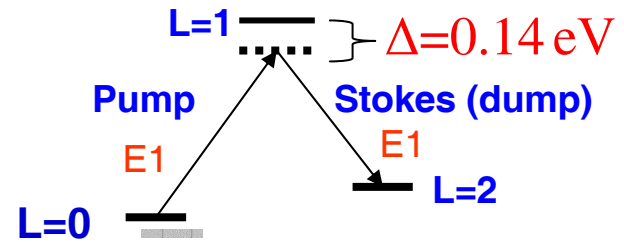


K. Eckert et al, PRA,  
70, 023606 (2004)

But detrimental non-linear impact of interaction between BEC atoms!

# Atomic clusters: off-resonant stimulated Raman transfer to the quadrupole 1eh state at 0.8 eV

$e_{eh} = e_h - e_e \longrightarrow$  Direct access to s-p spectra!



$\omega_{\text{pump}} = 1.25 \text{ eV}, \quad \omega_{\text{stokes}} = 0.45 \text{ eV}$

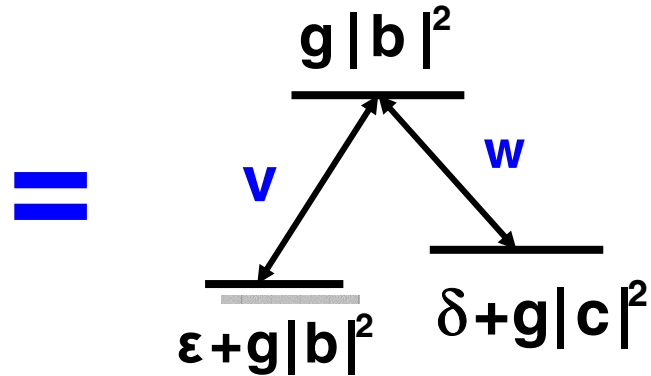
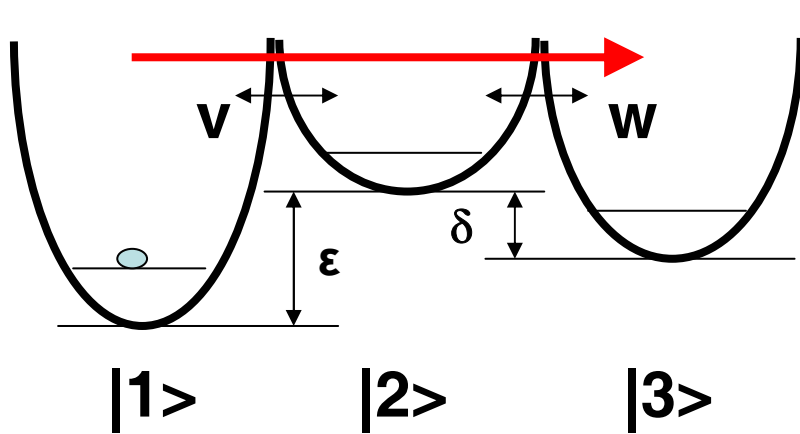
$T_s = T_p = 200 \text{ fs}, \quad T_{\text{shift}} = 0$   
 $I_s = 2.2 \times I_p = 2.2 \times 10^{10} \text{ W/cm}^2$

- Time-dependent HF
- Kohn-Sham functional
- LDA Perdew-Wang xc
- jellium for ions

ORSR works! But maybe low population?  
**STIRAP?** **SCRAP!**

# STIRAP transport of BEC between the wells

E.M. Graefe et al, PRA, 73, 013617 (2006)



**Analog of STIRAP!**

$$\psi(t) = a(t) |1\rangle + b(t) |2\rangle + c(t) |3\rangle$$

$$H(|a|^2, |b|^2, |c|^2) \begin{pmatrix} a \\ b \\ c \end{pmatrix} = i\hbar \frac{d}{dt} \begin{pmatrix} a \\ b \\ c \end{pmatrix}$$

$$H(|a|^2, |b|^2, |c|^2) = \begin{pmatrix} \epsilon + g|a|^2 & v & 0 \\ v & g|b|^2 & w \\ 0 & w & \delta + g|c|^2 \end{pmatrix} \approx H_{\text{STIRAP}} = \begin{pmatrix} -2\Delta_P + S_1 & \Omega_P & 0 \\ \Omega_P & S_2 & \Omega_S \\ 0 & \Omega_S & -2\Delta_S + S_3 \end{pmatrix}$$

The parameters  $v, w, \epsilon, \delta$  can be varied by controlling the depths or separations of the wells.

## BEC/STIRAP model:

$\hat{\psi}_k^\dagger(\vec{r}, t)$  -creates atom in component k at point r in time t

Equations for 3-component BEC:

$$i\hbar \frac{\partial}{\partial t} \hat{\psi}_k = [\hat{h}_k + \sum_{j=1}^3 g_{kj} \hat{\psi}_j^\dagger \hat{\psi}_j] \hat{\psi}_k + \sum_{j=1}^3 (1 - \delta_{kj}) \Omega_{kj}(t) \hat{\psi}_j$$

$g_{kj}$  - interaction

$\Omega_{kj}(t)$  - coupling

Transfer to macroscopic order parameters  $\psi_k(t)$  : GPE

$$\hat{\psi}_k^\dagger(\vec{r}, t) \simeq \psi_k(t) \Phi_k(\vec{r}), \quad \psi_k(t) = \sqrt{N N_k(t)} \exp\{-i\varphi_k(t)\}$$

$N_k(t)$  - normalized population

$\varphi_k(t)$  - phase

Equations for phases and populations:

$$\left\{ \begin{array}{l} \frac{\partial}{\partial t} N_k = - \sum_{j=1}^3 \bar{\Omega}_{kj}(t) \sqrt{N_j N_k} \sin(\varphi_k - \varphi_j) \\ \frac{\partial}{\partial t} \varphi_k = E_k + \sum_{j=1}^3 \Lambda_{kj} N_j - \frac{1}{2} \sum_{j=1}^3 \bar{\Omega}_{kj}(t) \sqrt{\frac{N_j}{N_k}} \cos(\varphi_k - \varphi_j) \end{array} \right.$$

$$\Omega_{kj}(t) = K \bar{\Omega}_{kj}(t)$$

$$\bar{\Omega}_{kj}(t) = \exp\left\{-\left(\frac{t_{kj} - t}{\Gamma}\right)^2\right\}$$

$$\bar{E}_k = E_k / 2K, \quad 2Kt \rightarrow t$$

$$U_{kj} \sim g_{kj}$$

Scaled dimensionless time

The only parameter regulating Interaction-coupling ratio

$$\Lambda_{kj} = \frac{U_{kj} N}{2K}$$

**Classical** Hamiltonian and canonical equations:

$$H_{CL} = \sum_{k=1}^3 \bar{E}_k + \frac{1}{2} \sum_{k,j=1}^3 \Lambda_{kj} N_j N_k - \frac{1}{2} \sum_{j=1}^3 \bar{\Omega}_{kj}(t) \sqrt{N_j N_k} \cos(\varphi_k - \varphi_j)$$

$$\left\{ \begin{array}{l} \frac{\partial}{\partial t} N_k = - \frac{\partial H_{cl}}{\partial \varphi_k} \\ \frac{\partial}{\partial t} \varphi_k = \frac{\partial H_{cl}}{\partial N_k} \end{array} \right.$$

**Canonical** transformation to new unknowns:

$$\left\{ \begin{array}{l} z_k = \sum_{j=1}^3 T_{kj} N_j \quad \text{- population imbalances} \\ \theta_k = \sum_{j=1}^3 R_{kj} \varphi_j \quad \text{- phase differences} \end{array} \right. \quad T = \begin{pmatrix} -1 & 1 & 0 \\ 0 & -1 & 1 \\ 1 & 1 & 1 \end{pmatrix}$$

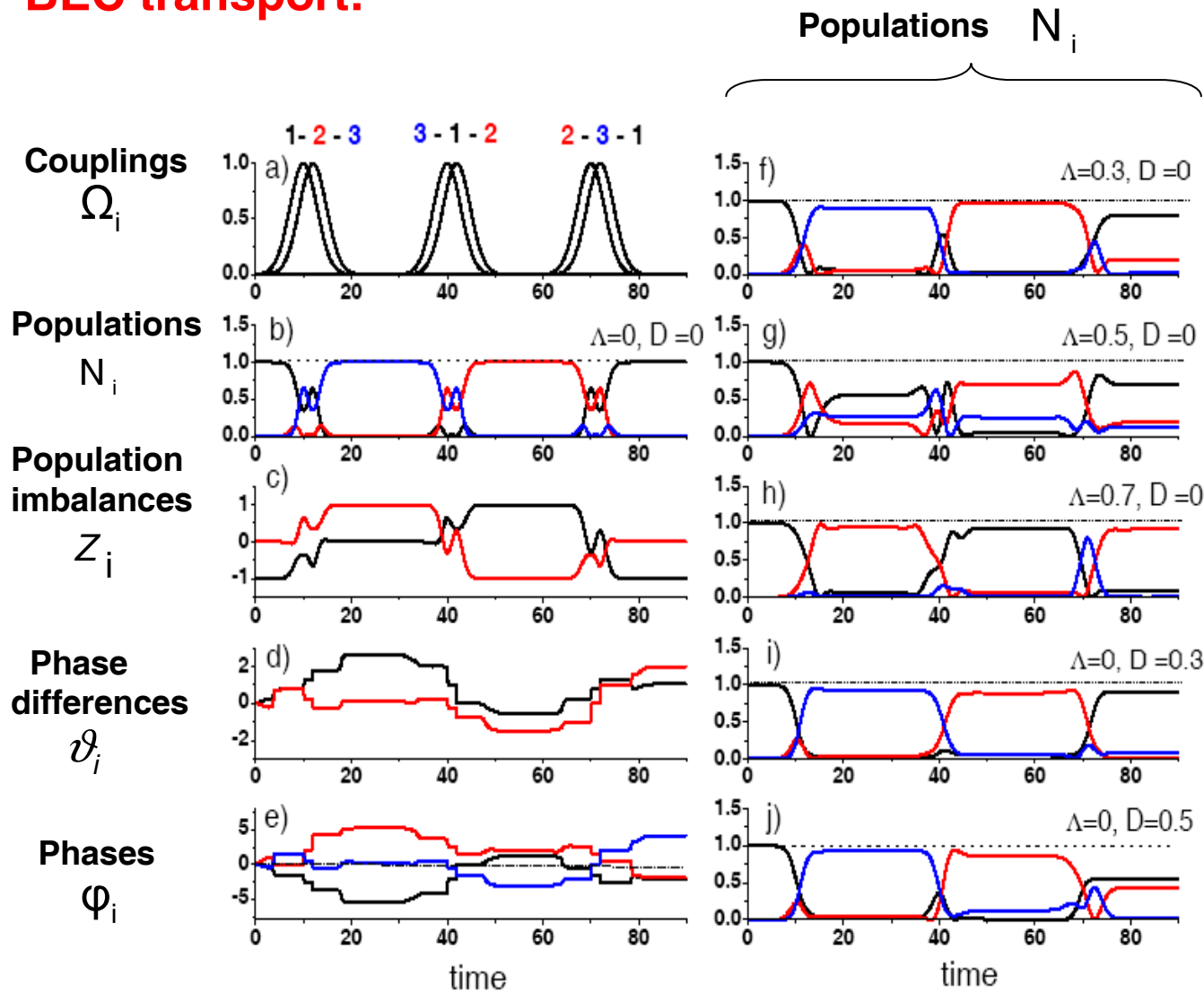
$$R = \frac{1}{3} \begin{pmatrix} -2 & 1 & 1 \\ -1 & -1 & 2 \\ 1 & 1 & 1 \end{pmatrix}$$

so as to **extract integrals of motion**  $N = \sum_{k=1}^3 N_k(t)$  and  $\Theta = \sum_{k=1}^3 \varphi_k(t)$

and to reduce 6 equations to 4 ones

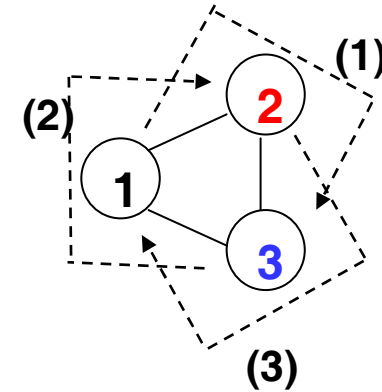


# BEC transport:



-- well 1  
 -- well 2  
 -- well 3

Circular well config.



**STIRAP:**  
 - complete at  $\Lambda=D=0$   
 - still survives at  $\Lambda, D < 0.5$

$$\Lambda_{kj} = \frac{U_{kj} N}{2K}$$

**STIRAP takes place even under (modest) interaction and so can be applied to realistic BEC!**

**Geometric phases!**

# Conclusions and Outlook

Particular two-photon population transfer methods can be applied to:

**atomic clusters: ORSR, 1eh modes, s-p electron spectra**

**Single-particle** (mean field) spectra

- sensitive to cluster structure and thus deliver info on diverse cluster features,
- robust test for theory,

STIRAP??  
**SCRAP!**

**BEC: STIRAP transport in multi-well traps**

**Perspectives:**

- **geometric phases,**
- **quantum informatics (STIRAP of atoms),**
- **multi-component BEC, ...**

1-photon, 2-photon, multiphoton population transfer schemes

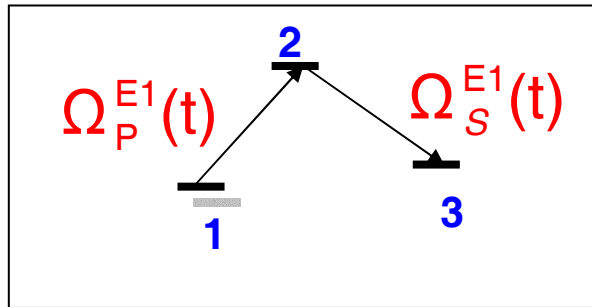
Thanks to similarity between multi-photon and tunneling schemes

Methods of modern  
quantum optics

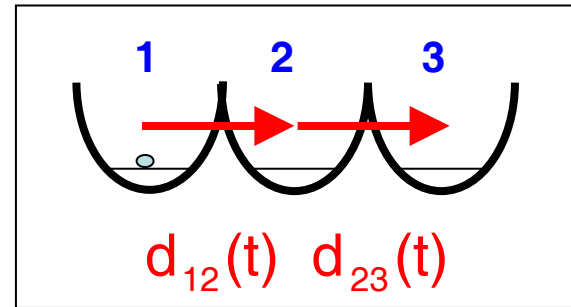


-Spectroscopy of atomic clusters  
- Transport of BEC, atoms, ...  
- ...

Equations describe **two scenarios**:

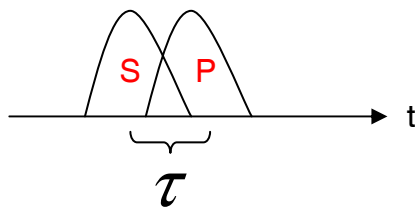


- **Three**-component BEC in **single**-well trap,
- coupling by pump and Stokes laser pulses,
- $U_{k \neq j} = U_{k=j} = U$

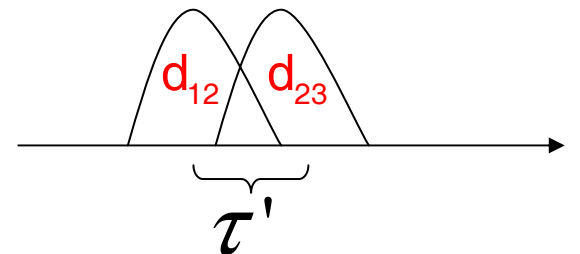


- **One**-component BEC in **triple**-well trap,
- coupling via barriers between traps,
- $U_{k \neq j} = 0, \quad U_{kk} = U$

**Adiabatic condition:**



$$\Omega \tau > 10$$



$$2K\tau = \tau', \quad \Omega \tau = K\tau = 0.5\tau' > 10,$$

$$\tau' > 20$$

- very simple form

# Atomic clusters



## Spectra of valence electrons:

1) **collective modes (plasmons)**

2) **infrared 1eh excitations**

$$e_{eh} = e_h - e_e$$

3) **Single-particle (mean field) spectra**

- sensitive to cluster structure and thus deliver info on diverse cluster features,
- robust test for theory,
- still poorly studied, hot topic!

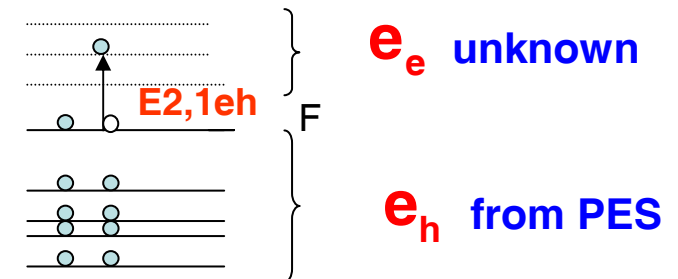
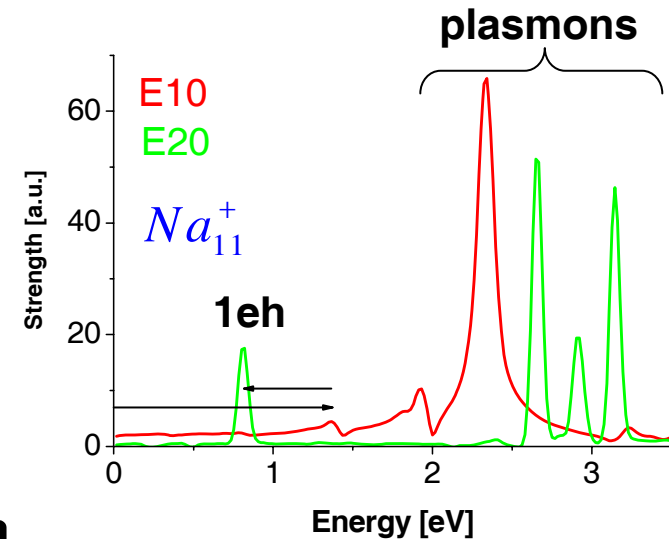


**Infrared 1eh modes provide direct access to s-p spectrum above Fermi level**



### Problems:

- very short lifetimes (10-1000 fs) →
- strong dynamical Stark shifts ←
- competition with plasmons



**intense lasers with ultra-short (fs) pulses**

## Model:

- Kohn-Sham functional, Perdew-Wang xc
- Time Dependent Local Density Approximation (TDLDA)
- propagation of single-electron wave function in time
- including photoemission through absorption boundary
- expectation values of multipole moments
- Fourier transformation into frequency domain
- coherent (classical) laser field

$$i\hbar \frac{\partial}{\partial t} \phi_i(\vec{r}, t) = \hat{h}_{KS}(\vec{r}, t) \phi_i(\vec{r}, t)$$

$$D(t) = \int d\vec{r} r^L Y_{L0}(\Omega) \rho(\vec{r}, t)$$

$$\tilde{D}(\omega) = \int dt e^{i\omega t} D(t)$$

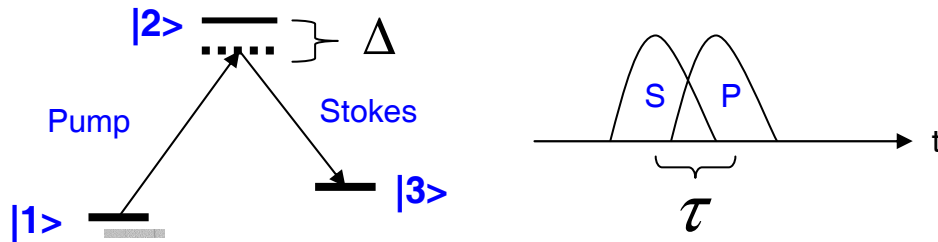
$$\mathbf{E}(t) \cos(\omega t), \quad \mathbf{E}(t) = \sin^2(t/T), \quad T = 100 - 500 \text{ fs}$$

- axially deformed cluster  $Na_{11}^+$
- quadrupole (LM=20) infrared 1eh state at 0.75 eV
- jellium approximation for ions

V.O. Nesterenko, W. Kleinig, P.-G. Reinhard, and D.S. Dolci, Phys. Rev. A70, 023205 (2004);  
V.O. Nesterenko, P.-G. Reinhard, Th. Halfmann and L.I. Pavlov, Phys. Rev. A73, 02120 (2006);  
V.O. Nesterenko, P.-G. Reinhard, Th. Halfmann and E. Suraud, J. Phys. B, 39, 3905 (2006).

# STImulated Raman Adiabatic Passage (STIRAP): basic points

K. Bergman, et al,  
Rev. Mod. Phys., 70, 1003 (1998)



STIRAP provides up to 100% of the population transfer!

## Main requirements:

- **Two-photon resonance:**  $\omega_p = \omega_2 - \omega_1 - \Delta$ ,  $\omega_s = \omega_2 - \omega_3 - \Delta \implies \omega_p - \omega_s = \omega_3 - \omega_1$
- **Overlapping pulses, counterintuitive order**
- **Adiabatic evolution:**  $\Omega\tau > 10$
- **Dark state, no contribution from |2> at all!**

$$\Omega = \sqrt{\Omega_P^2 + \Omega_S^2}$$

- Rabi frequency

System of equations for **dressed** states  $|a \rangle$ :

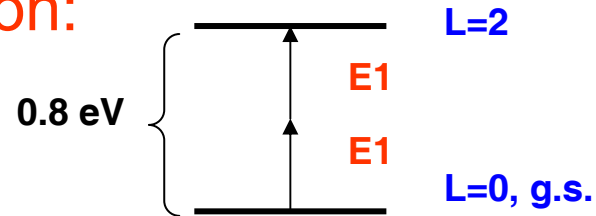
$$\begin{cases} |a^+ \rangle = \sin \theta \sin \phi |1 \rangle + \cos \phi |2 \rangle + \cos \theta \sin \phi |3 \rangle \\ |a^0 \rangle = \cos \theta |1 \rangle + \sin \theta |3 \rangle \\ |a^- \rangle = \sin \theta \cos \phi |1 \rangle + \sin \phi |2 \rangle + \cos \theta \cos \phi |3 \rangle \end{cases}$$

STIRAP dark state.  
Maximal population at  $\tau > 0$ .

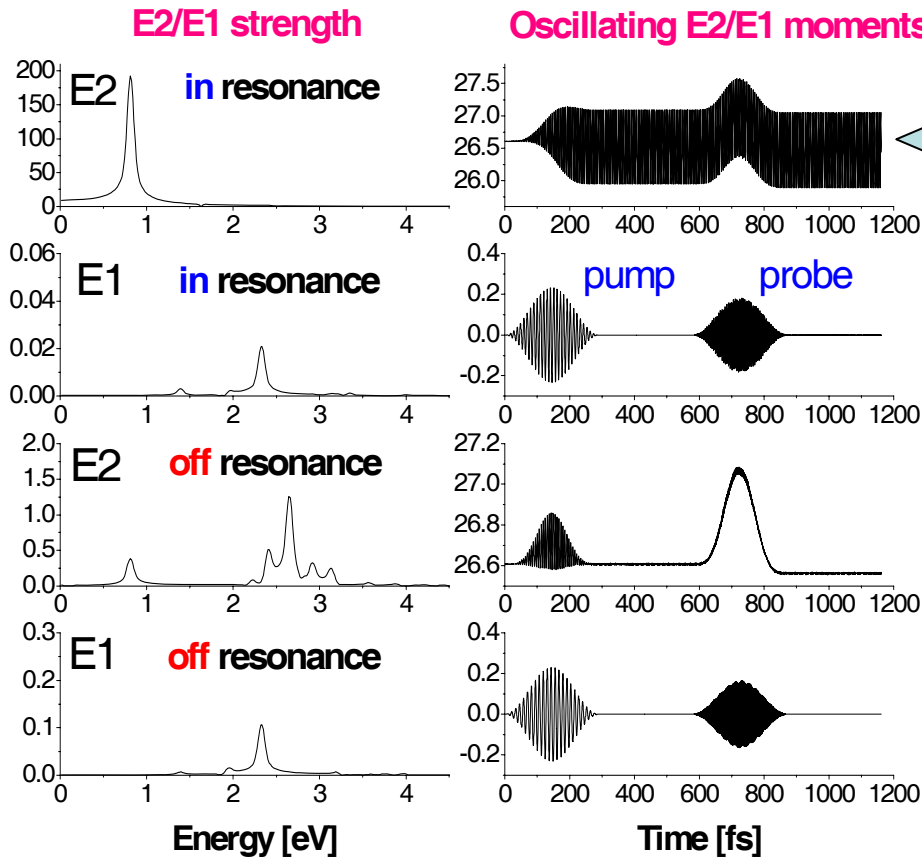
$$\sin \theta = \frac{\Omega_P}{\sqrt{\Omega_P^2(t) + \Omega_S^2(t)}}, \quad \cos \theta = \frac{\Omega_S}{\sqrt{\Omega_P^2(t) + \Omega_S^2(t)}}, \quad \omega^\pm = \Delta \pm \sqrt{\Delta^2 + \Omega_P^2 + \Omega_S^2}, \quad \omega^0 = 0$$

# Direct two-photon population:

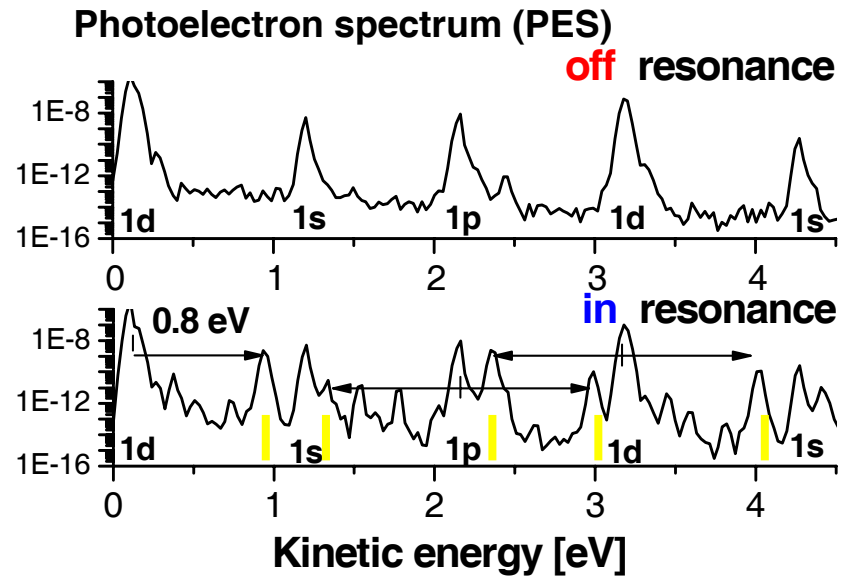
Measuring 1eh energy and lifetime



$\text{Na}_{11}^+$   
jellium TDLDA

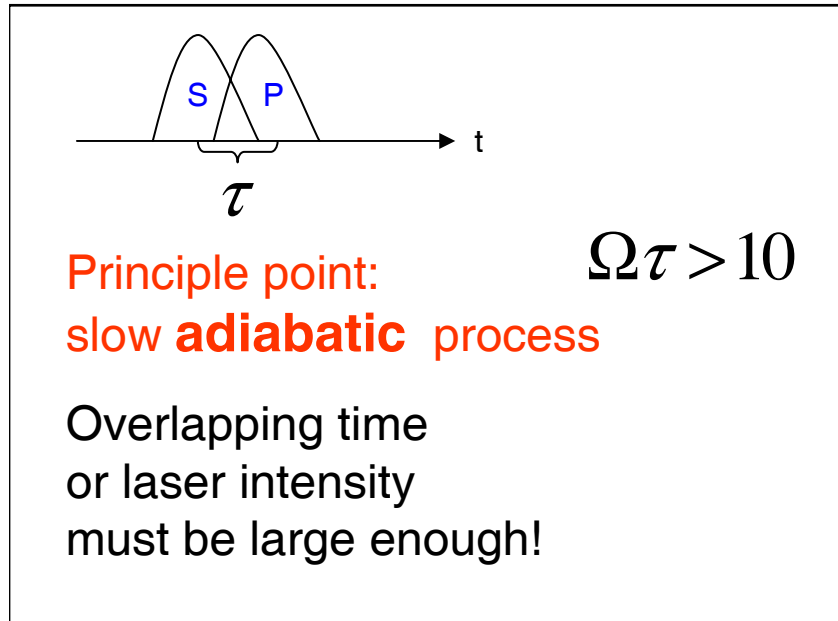


Endurant quadrupole oscillations result in PES satellites:



Probe pulse follows the pump pulse with a large delay 600 fs so as to detect only the endurant quadrupole mode

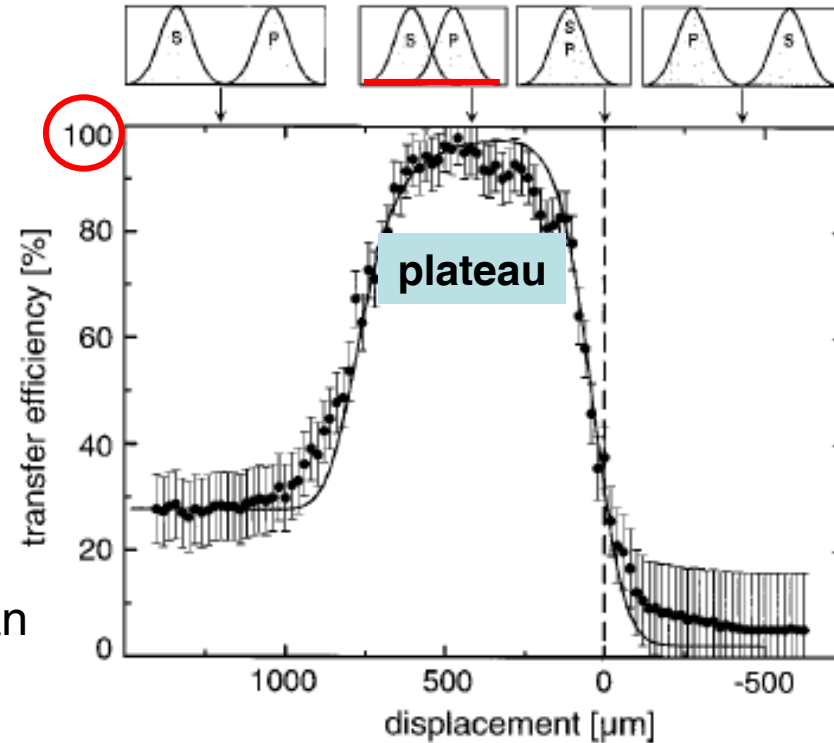
$I = 10^{11} \text{ W/cm}^2$ ,  $T = 300 \text{ fs}$   
 $\omega_{\text{pump}} = 0.40 \text{ eV}$  (in res.),  $0.34 \text{ eV}$  (off res.)  
 $\omega_{\text{probe}} = 3.1 \text{ eV}$



$$\Omega\tau > 10$$

Maximal limit for  
stimulated Raman

Population transfer between  $^3P_0$  and  $^3P_2$  states in Ne atom



Plateau:

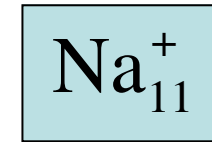
The process is only sensitive  
slightly sensitive to variation  
of laser parameters.

- Principle signature of STIRAP:  
maximal population with plateau at  
counterintuitive order of pulses



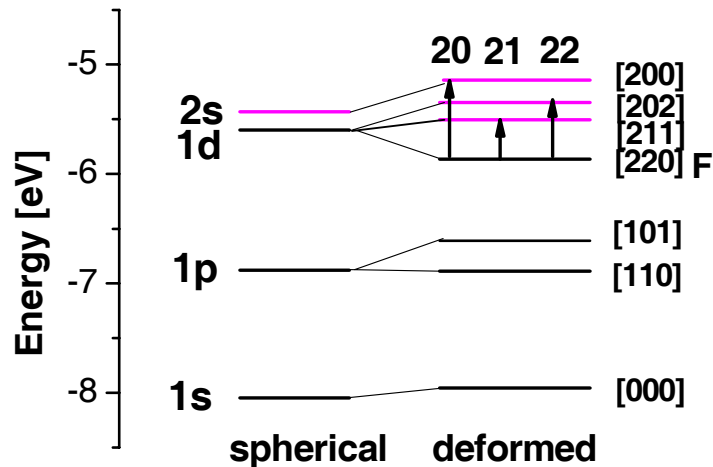
## Advantages of light deformed clusters:

- safe size selection, well known shape, routinely available beams
- dilute infrared 1eh spectra,



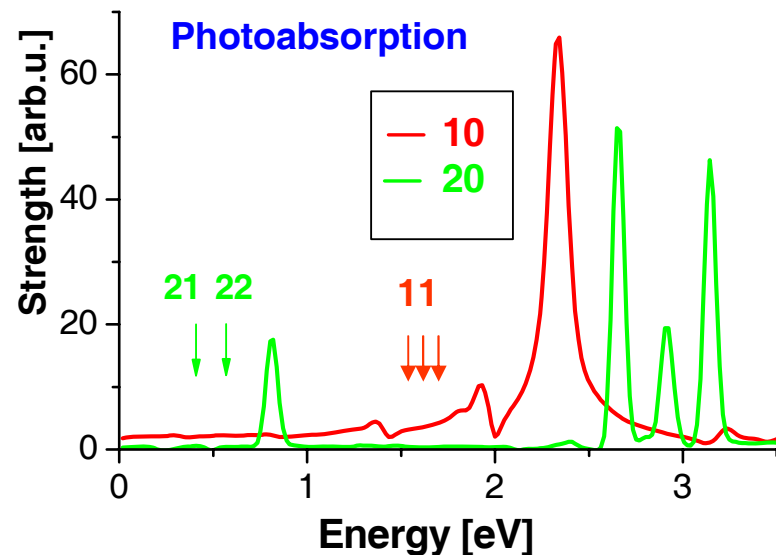
prolate, axial

### Single-electron spectrum



-- 21 and 22 1eh-modes are fully driven by cluster deformation

V.O. Nesterenko, P.-G. Reinhard, W. Kleinig, and D.S. Dolci, PRA, v.70, 023205 (2004).



Every infrared quadrupole mode is strictly dominated by one 1eh configuration:

E20:	[220]-[200]	99.9%
E21:	[220]-[211]	99.5%
E22:	[220]-[202]	99.6%

Access to:  
 -- cluster mean field  
 -- deformation effects

$\tau_{1eh} = 1-5 \text{ ps}$   $\Rightarrow$  fs intense lasers in TPP!